

of model solids characterizing the elasticity of those materials. In transforming the elasticity of the Earth into solid-state parameters of composition, pressure, and temperature, the properties needed are the intrinsic elastic properties of earth materials (not the apparent properties as one measures on a porous sample).

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### Notation

| <i>Symbols</i> | <i>Units</i> | <i>Meaning</i>                                          |
|----------------|--------------|---------------------------------------------------------|
| $V_p$          | km/sec       | Velocity of compressional waves                         |
| $V_p^0$        | km/sec       | Velocity of compressional waves at zero-porosity        |
| $V_s$          | km/sec       | Velocity of shear waves                                 |
| $V_s^0$        | km/sec       | Velocity of shear waves at zero-porosity                |
| $V_j$          | km/sec       | Velocity of <i>j</i> th mode                            |
| $M_j$          | kb           | Elastic modulus of <i>j</i> th mode                     |
| $M_j^0$        | kb           | Elastic modulus of <i>j</i> th mode at zero-porosity    |
| $L_s$          | kb           | Longitudinal modulus given by (density $\times V_p^2$ ) |
| $L_s^0$        | kb           | Longitudinal modulus at zero-porosity                   |
| $\mu$          | kb           | Shear modulus                                           |
| $\mu^0$        | kb           | Shear modulus at zero-porosity                          |
| $K_s$          | kb           | Adiabatic bulk modulus                                  |
| $K_s^0$        | kb           | Adiabatic bulk modulus at zero-porosity                 |
| $K_T$          | kb           | Isothermal bulk modulus                                 |
| $K_T^0$        | kb           | Isothermal bulk modulus at zero-porosity                |
| $Y$            | kb           | Young's modulus                                         |
| $\sigma_s$     | None         | Poisson's ratio                                         |
| $\sigma_s^0$   | None         | Poisson's ratio at zero-porosity                        |
| $f_j$          | Hz/sec       | Pulse-repetition frequency (PRF) of <i>j</i> th mode    |

|          |        |                                 |
|----------|--------|---------------------------------|
| $f_p$    | Hz/sec | PRF of compressional mode       |
| $f_s$    | Hz/sec | PRF of shear mode               |
| $P$      | None   | Compressional mode              |
| $S$      | None   | Shear mode                      |
| $a$      | None   | Aspect ratio                    |
| $p$      | kb     | Pressure                        |
| $T$      | °K     | Temperature                     |
| $\alpha$ | per °K | Coefficient of volume expansion |
| $\theta$ | None   | Volume fraction of pores.       |

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